Physics of atoms and molecues

Quiz 1

1. Show how the vector potential amplitude  $A_0$  would change if the number density of photon  $n(\omega)$  doubles for given  $\omega$ .[2]

Hint:  $A_0(\omega) = \sqrt{rac{n(\omega)\hbar}{2\omega\epsilon_0}}$ ; start with the expression of field energy density

2. For  $\vec{A}(\vec{r},t) = \vec{A}_0 e^{i\vec{k}.\vec{r}}\delta(t)$  show what will be the ratio of  $E_0(\omega)$  and  $E_0(2\omega)$  and also of  $I(\omega)$  and  $I(2\omega)$ .[2+2]

Hint: Delta pulse means all  $A_0(\omega)$  for all  $\omega$  has same value. Use :  $E_0 = -2\omega A_0(\omega)\hat{E}$ ;  $\rho(\omega) = 2\epsilon_0\omega^2 A_0(\omega)$  derive and use in  $I(\omega)$ .

3. Consider two molecules which are exposed to perfect light pulse described by the  $\vec{A}(\vec{r}, t)$  given in question 2, are undergoing transition, one from energy levels 1 Hartree to 3 Hartree and the other from 2 Hartree to 4 Hartree (remember atomic units) respectively. If the maximum transition rates in the two transitions are same then what can you infer about the corresponding dipole transition matrix elements.[3]

Hint: Use  $W_{ba}^D = \frac{\pi^2}{\hbar c} \frac{e^2}{4\pi\epsilon_0} I(\omega_{ba}) |\vec{r}_{ba}| \cos^2\theta$ ; choose  $\theta$  for max W; get  $I(\omega)$  as above.

If a system, let us say the first one, rotates in the plane perpendicular to the direction of propagation of light with an angular velocity  $\omega_1$  then schematically plot the absorption spectra.[2]

Hint : the  $cos^2\theta$  in expression of  $W^D$ .

What will be ratio of the absorption cross-sections of the two processes described above ?[3]

Hint:  $\sigma = \frac{\hbar \omega_{ba} W_{ba}^D}{I(\omega_{ba})}$  sustitute  $I(\omega)$  from above and  $W^D$  as said.

4. Argue that in any system 2s states will have a large lifetime.[2]

Hint: 
$$\Delta l = \pm 1$$

5. Show that  $\Delta m = 0, \pm 1, \pm 2$  for the electric quadrupole transition term. [3]

Hint: Work out the azimuthal ( $\phi$ ) part of  $\langle l, m | r_i r_j | l \pm 1, m' \rangle$ , where  $r_{1,2,3} = x, y, z$ , using the spherical harmonics ; In class I have already showed for  $\langle b | xz | a \rangle$ .