

# Exploring The QCD Phase Diagram With High Energy Nuclear Collisions

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Outline:

QCD Phase Diagram

Experimental Study of QCD Phase Diagram

Conclusions

Symposium on Charm, Dileptons and Deconfinement  
April 4 - 8, 2011, Dresden, Germany

# Phase Transitions

Physical systems undergo phase transitions when external parameters such as the temperature ( $T$ ) or a chemical potential ( $\mu$ ) are tuned.

Systems following Quantum Chromodynamics (QCD) - No exception

	Associated chemical potential
Conserved Quantities: Baryon Number	$\sim \mu_B$
Electric Charge	$\sim \mu_Q \sim \text{small}$
Strangeness	$\sim \mu_S \sim \text{small}$

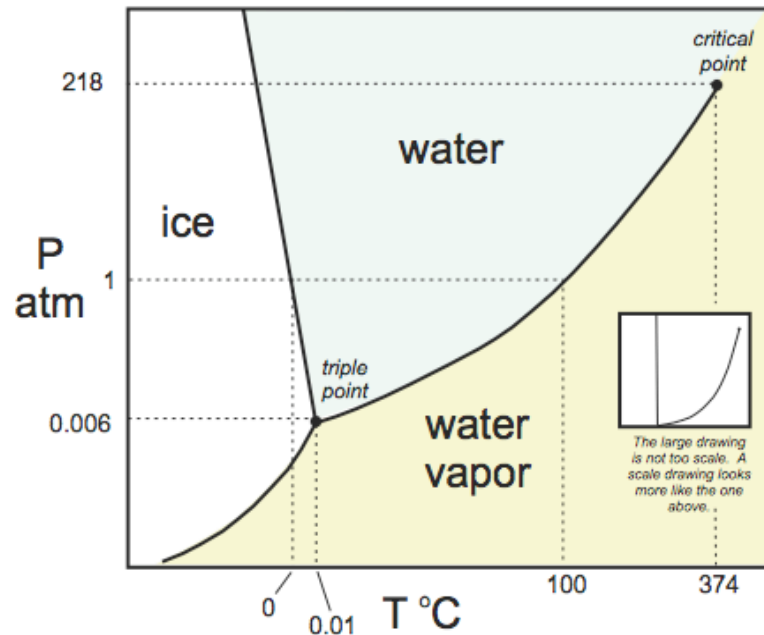
In principle a four dimensional phase diagram

A simpler version :  $T$  vs.  $\mu_B$

# QCD Phase Diagram

Phase diagram is a type of graph used to show the equilibrium conditions between the thermodynamically distinct phases

Water : Atomic  
Precisely known

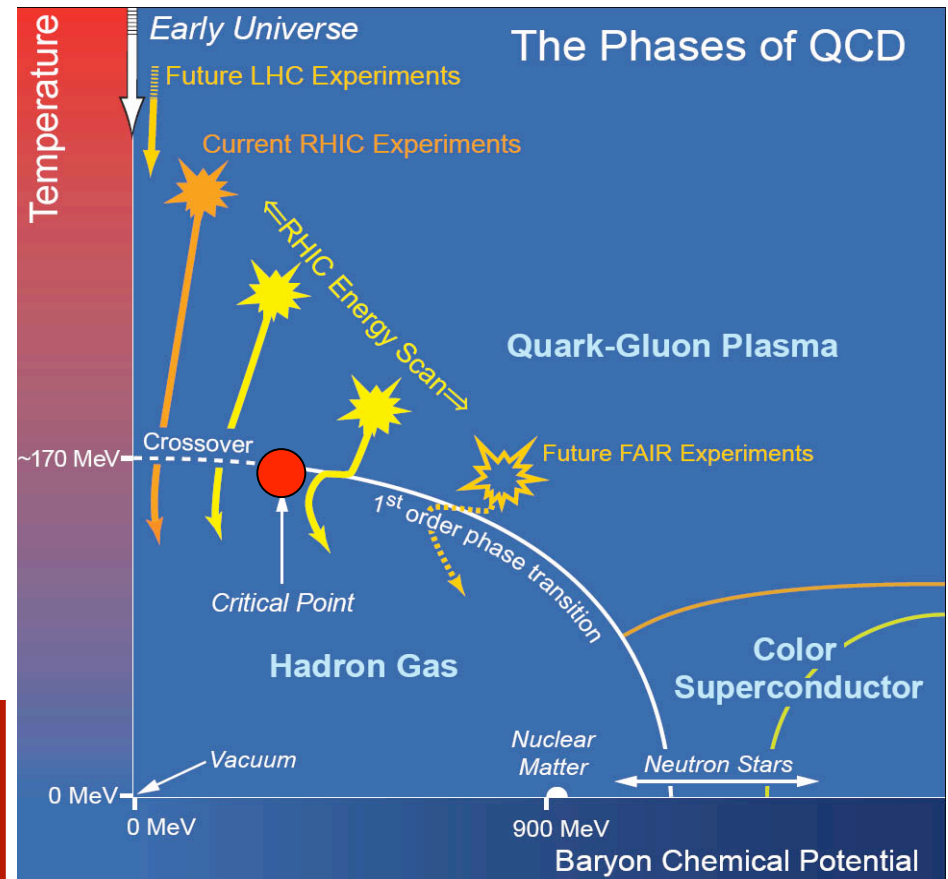


14 APRIL 2006 VOL 312 SCIENCE, Page 190

QCD phase diagram:  
Thermodynamics of bulk strongly  
interacting matter

QCD (Hadrons -- Partons)

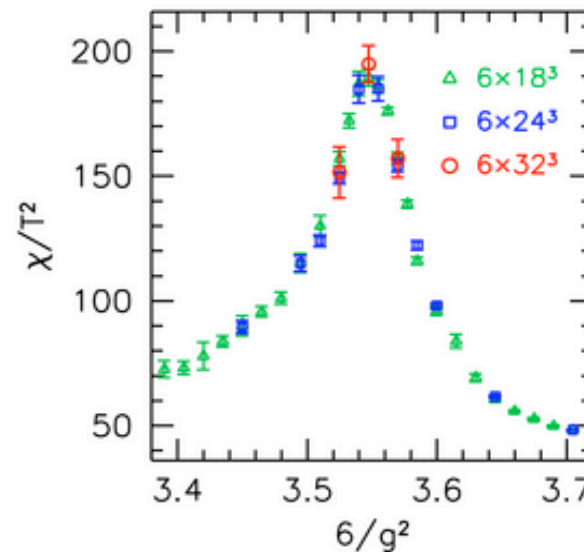
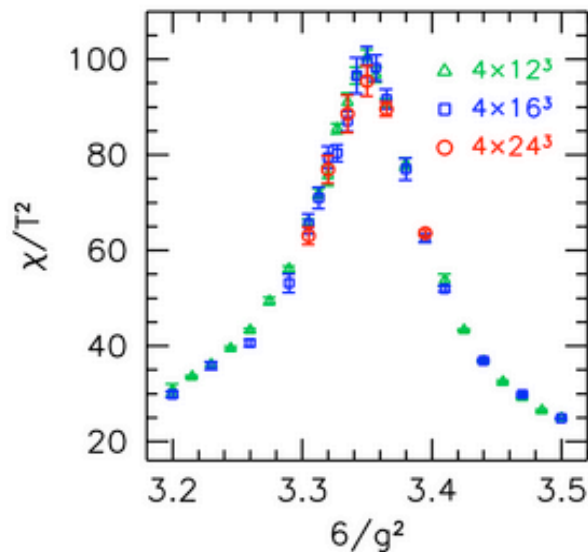
Theory and Experimental approaches



# Order Of Phase Transition at $\mu_B \sim 0$

$$\chi(N_g, N_t) = \partial^2 / (\partial m_{ud}^2) (T/V) \cdot \log Z$$

Y. Aoki et al., Nature443:675-678,2006



1<sup>st</sup> order :

Peak height  $\sim V$

Peak width  $\sim 1/V$

Cross over :

Peak height  $\sim \text{const.}$

Peak width  $\sim \text{const.}$

2<sup>nd</sup> order :

Peak height  $\sim V^\alpha$

No significant volume dependence (8 times difference in volumes)  
 Transition at high T and  $\mu_B = 0$  is a cross over

Lattice results on electroweak transition in standard model  
 is an analytic cross-over for large Higgs mass

K. Kajantie et al., PRL 77, 2887-2890,2006

# QCD Critical Point

*2nd order point in the PD, where the 1st order transition lines ends*

First Principle QCD Calculations on Lattice:

$$\langle \Theta(m_v) \rangle = \frac{\int DU \exp(-S_G) \Theta(m_v) \text{Det } M(m_s)}{\int DU \exp(-S_G) \text{Det } M(m_s)}$$

M : Dirac Matrix  
S<sub>G</sub> : Gluonic action

Issue for non zero  $\mu$ , Det M is not positive definite

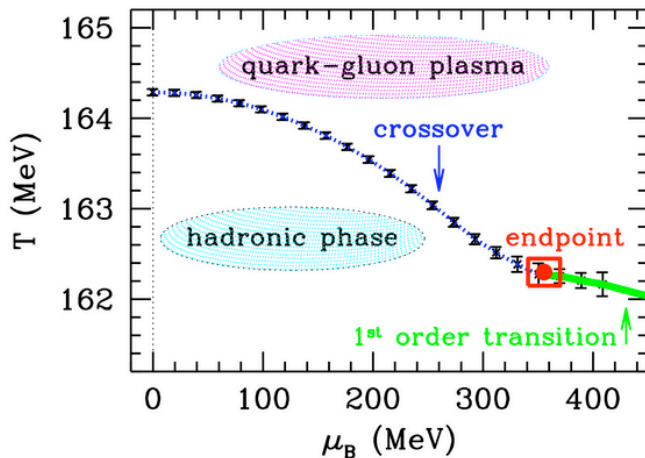
-- Sign problem

Reweighting

Taylor Expansion

Z. Fodor and S.D. Katz JHEP 0404, 50 (2004)

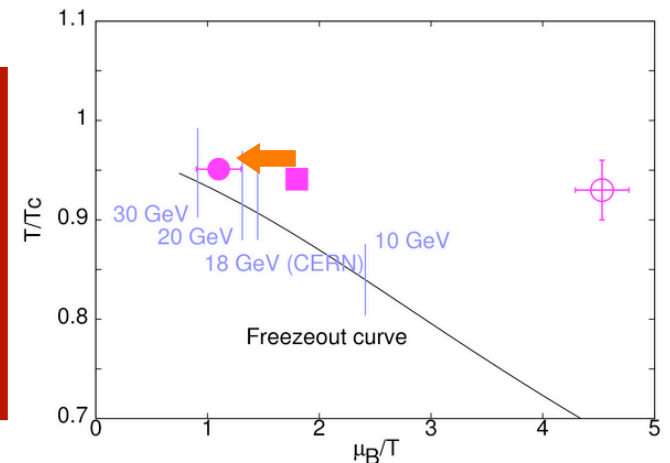
R. Gavai and S. Gupta Phys. Rev. D 78, 14503 (2008)



CP exists  
(in most QCD calculations )  
1<sup>st</sup> order transition  
at large  $\mu_B$

$$T_E = 162 \pm 2 \text{ MeV}$$

$$\mu_E = 360 \pm 40 \text{ MeV}$$



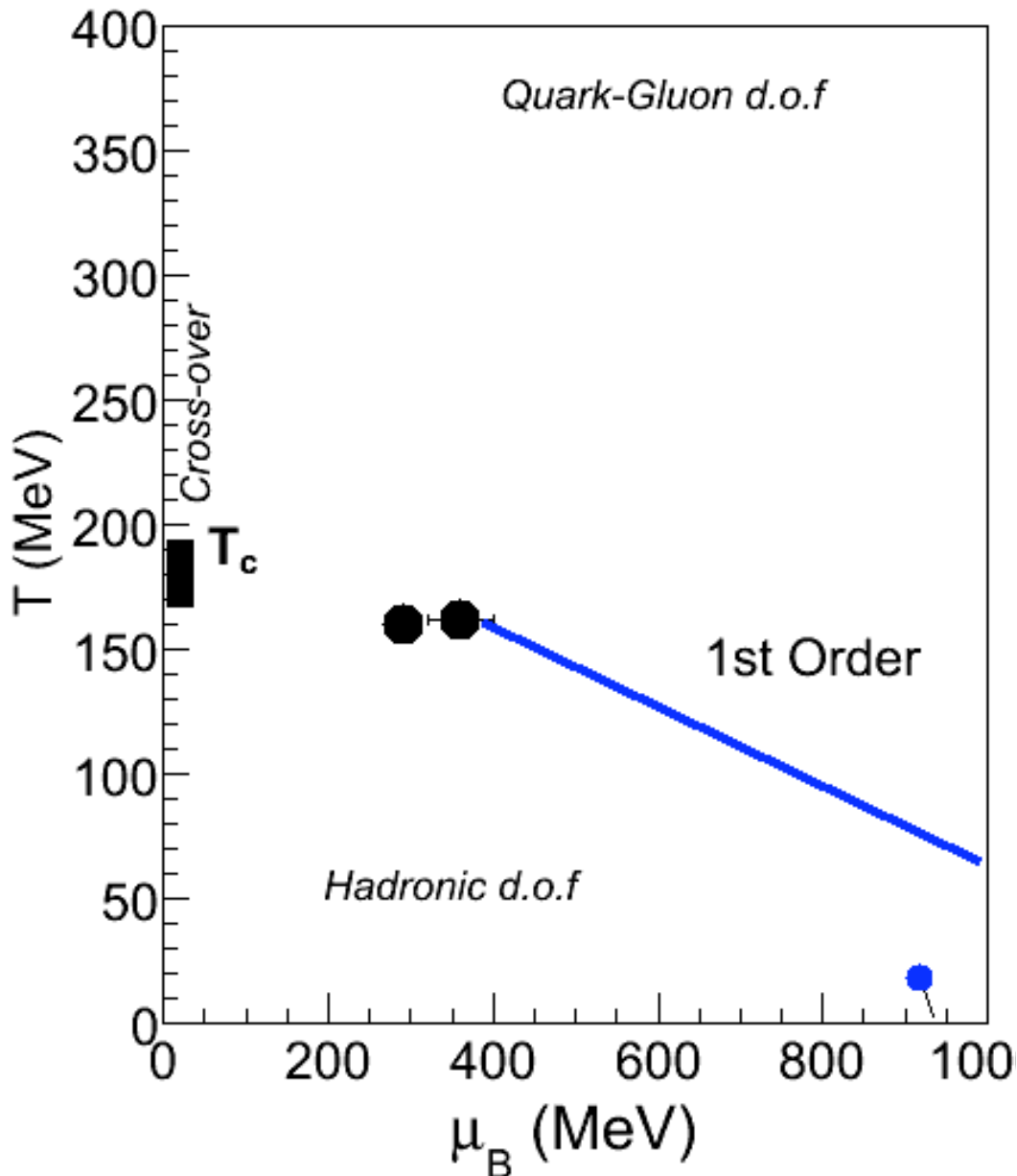
$$T_E/T_C = 0.94 \pm 0.01$$

$$\mu_E/T_E = 1.8 \pm 0.1$$

# QCD Phase Diagram: Theoretical

Tc: M. Cheng et al, Phys. Rev. D 74, 054507 (2006)

Y. Aoki et al, Phys. Lett. B 643, 46 (2006); 0903.4155



Lattice and other QCD based models :

$\mu_B = 0$  - Cross-over

$T_c \sim 170$ -195 MeV

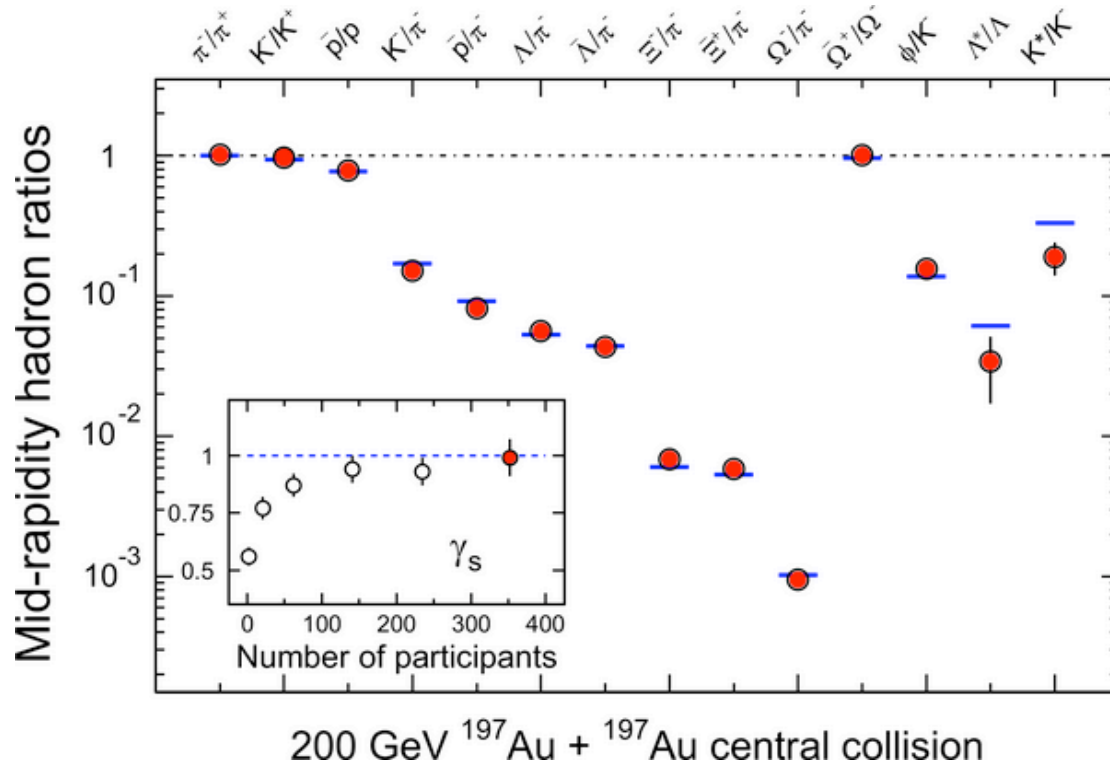
$\mu_B > 160$  MeV - QCD critical point

Experimental Study

- (i) How to access PD
- (ii) Tests of QCD
- (iii) Scale of PD
- (iv) Search Phase Boundary
- (v) Search CP

# Accessing Phase Diagram

P. Braun-Munzinger, J. Stachel,  
Nature 448:302-309,2007



○ data

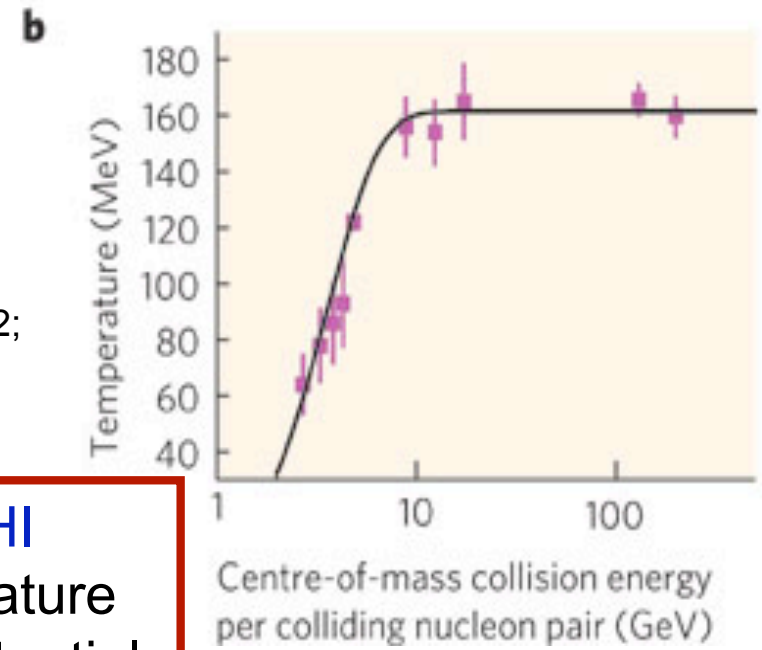
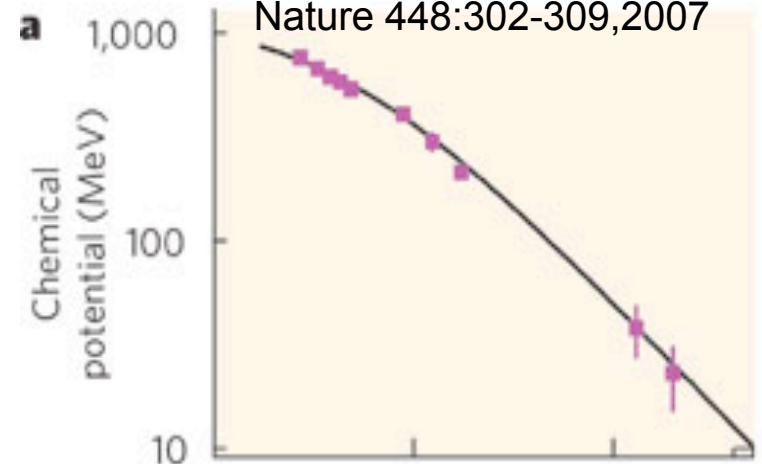
— Thermal model fits

$$T_{\text{ch}} = 163 \pm 4 \text{ MeV}$$

$$\mu_{\text{B}} = 24 \pm 4 \text{ MeV}$$

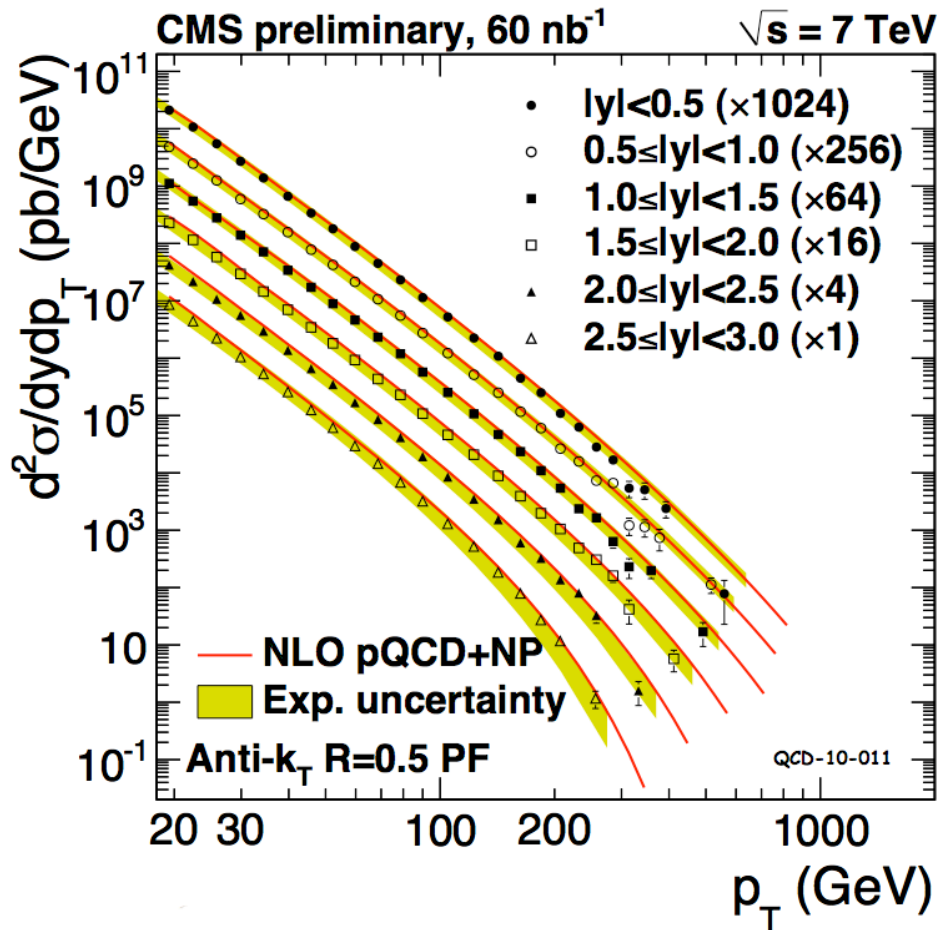
RHIC white papers - 2005,  
Nucl. Phys. *A757*, STAR: p102;  
PHENIX: p184.

Varying beam energy in HI collisions varies Temperature and Baryon Chemical Potential

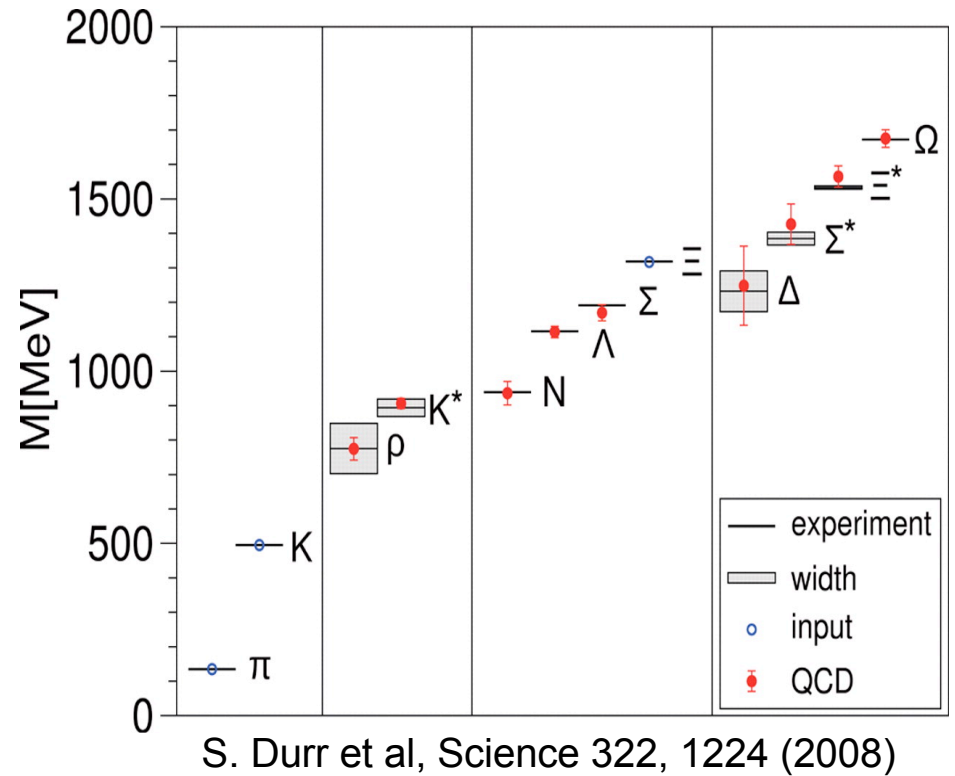


# Tests of QCD

Short distance  
perturbative regime



Long-distance  
Non-perturbative regime



Can we test of the QCD thermodynamics of bulk strongly interacting mater



# Tools for testing non-pQCD (T>0)

Theory

Lattice QCD

First principle QCD calculations  
in non-perturbative regime

$$\chi_2^X = \frac{1}{VT^3} \langle N_X^2 \rangle$$
$$\chi_4^X = \frac{1}{VT^3} (\langle N_X^4 \rangle - 3\langle N_X^2 \rangle^2)$$

$$[\chi^{(3)} T] / [\chi^{(2)} T^2] \sim \text{Skewness} \times \sigma$$
$$\chi^{(4)} / [\chi^{(2)} T^2] \sim \text{Kurtosis} \times \sigma^2$$
$$\chi^{(4)} / [\chi^{(3)} T] \sim \text{Kurtosis} \times \sigma / \text{Skewness}$$

Assumptions:

Net-proton  $\sim$  Net-baryon

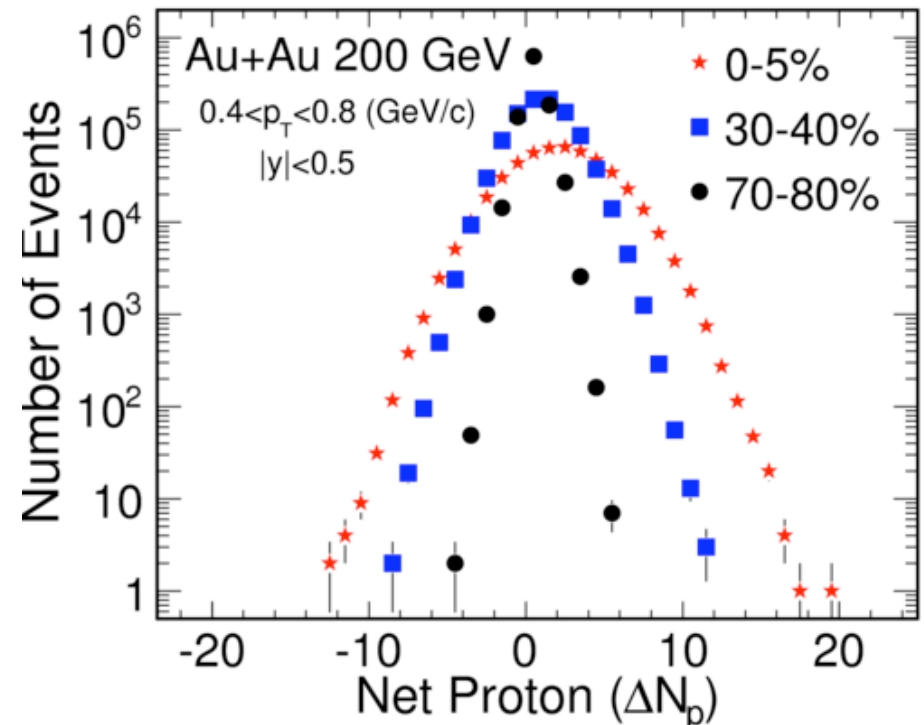
Thermal Equilibrium and Grand Canonical Ensemble

Freeze-out conditions

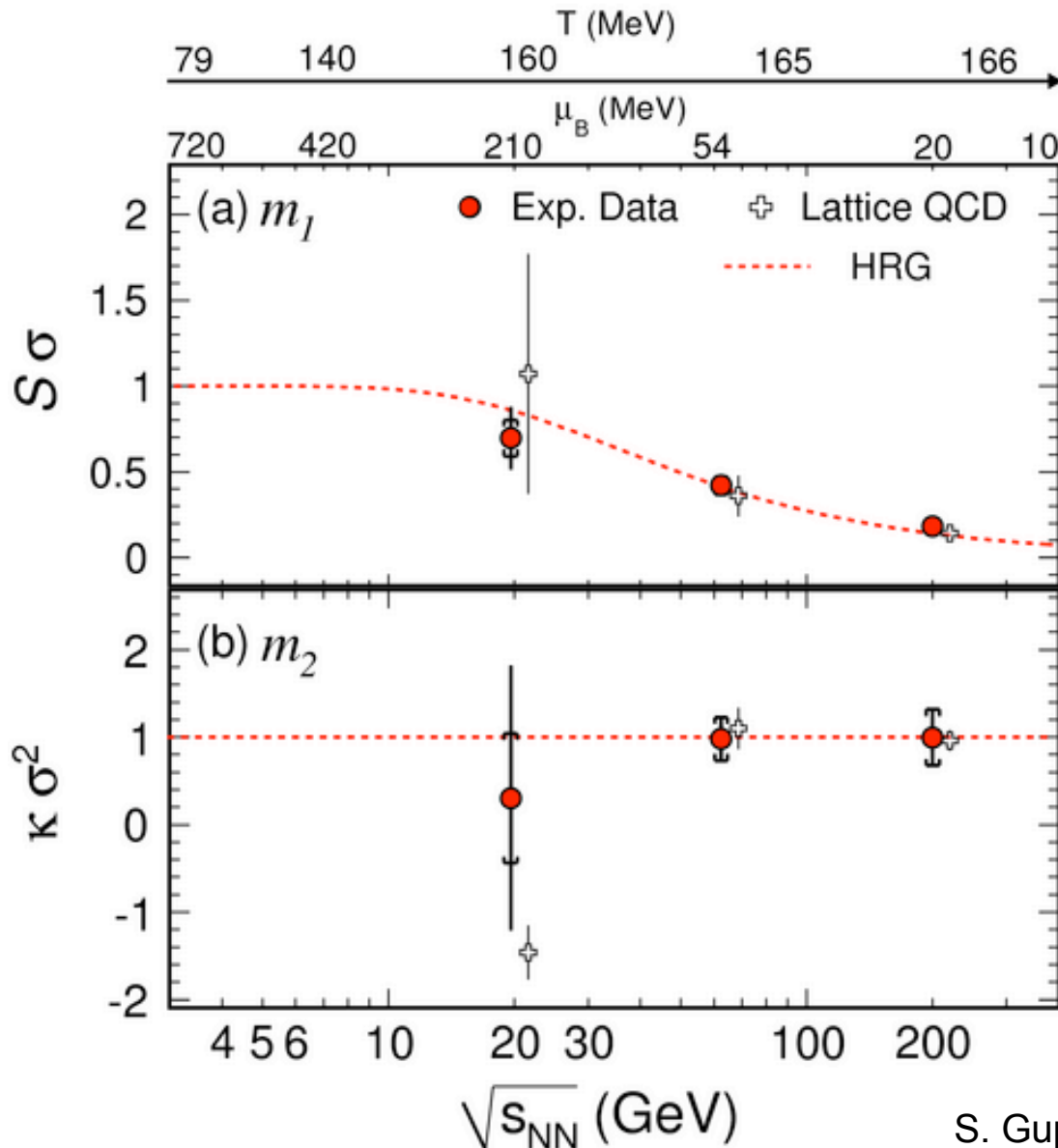
Lattice Systematics

Experiment

High Energy Heavy-ion collisions



# Test of QCD in non-perturbative regime



QCD vs. Expt. Data  
(both  $T > 0$ )  
in non-perturbative regime

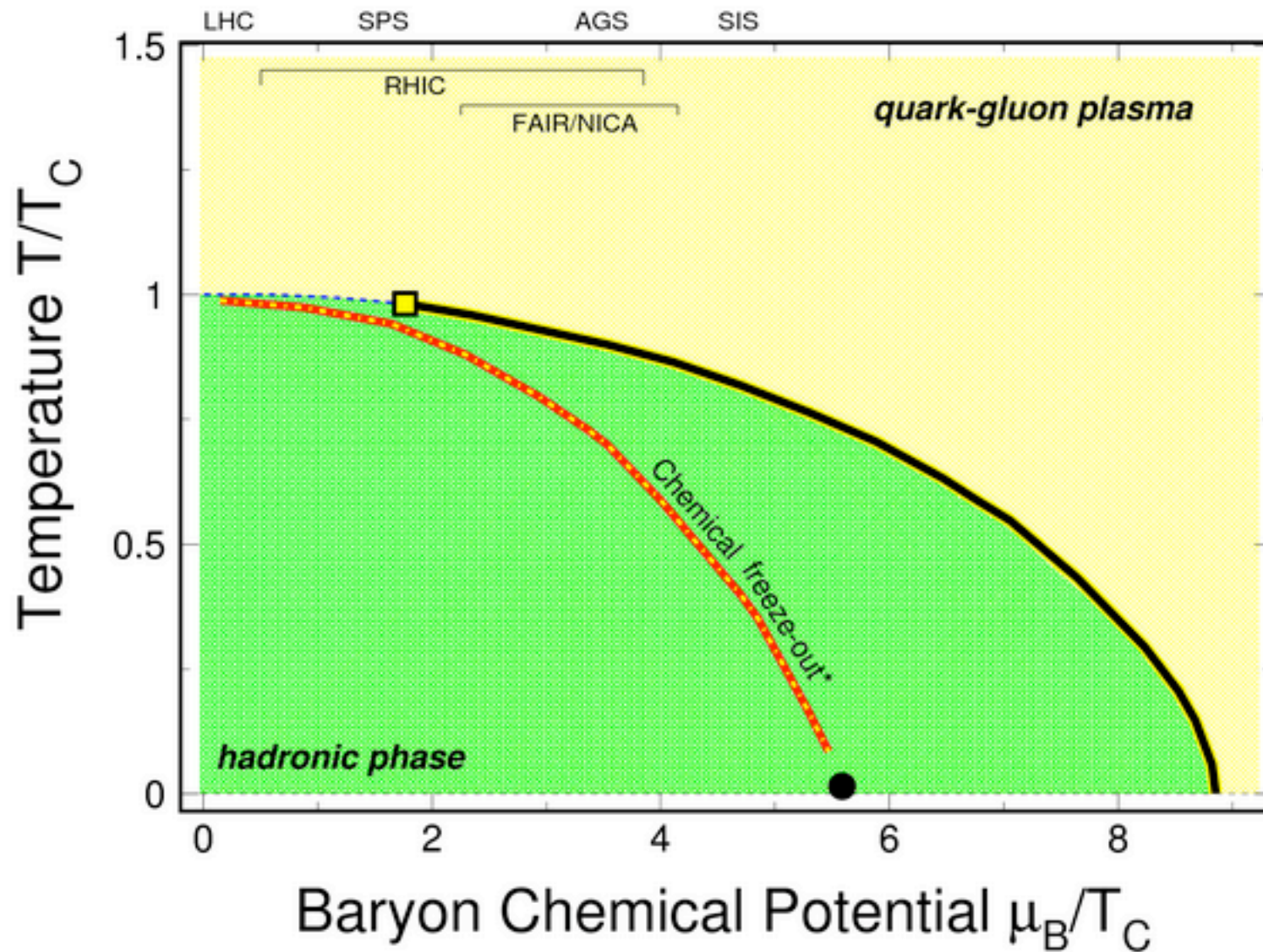
$T \chi^{(3)}/\chi^{(2)}$   
 $T^2 \chi^{(4)}/\chi^{(2)}$

Non-trivial indication  
(using fluctuations) that  
fireball produced in  
heavy-ion collisions  
attained thermal and  
chemical equilibrium at  
chemical freeze-out

R. Gavai & S. Gupta arXiv:1001.3796  
F. Karsch & K. Redlich PLB 695, 136 (2011)

S. Gupta, X. Luo, H. G. Ritter, BM, N. Xu

# Scale for the QCD phase diagram



$T_C$  sets the scale of the QCD phase diagram

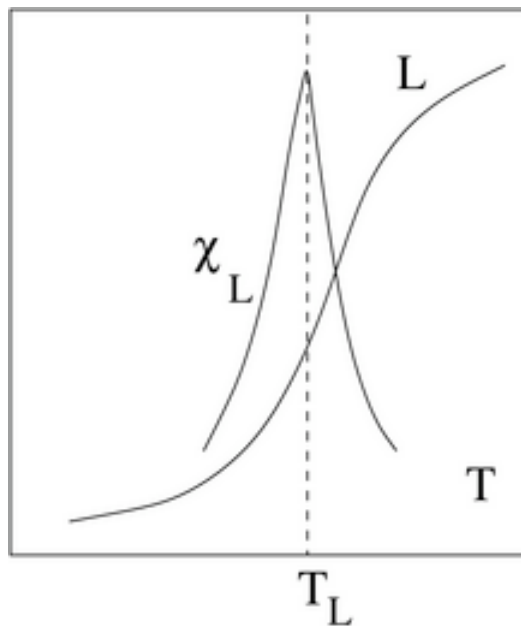
# Definition of $T_c$

Polyakov Loop

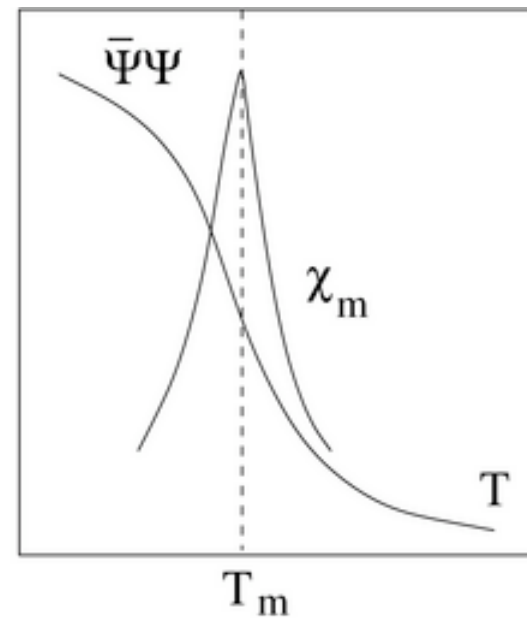
$$L(T) \sim \lim_{r \rightarrow \infty} \exp\{-F(r)/T\}$$

Susceptibility

$$\chi_L(T) \sim \langle L^2 \rangle - \langle L \rangle^2$$



(a)



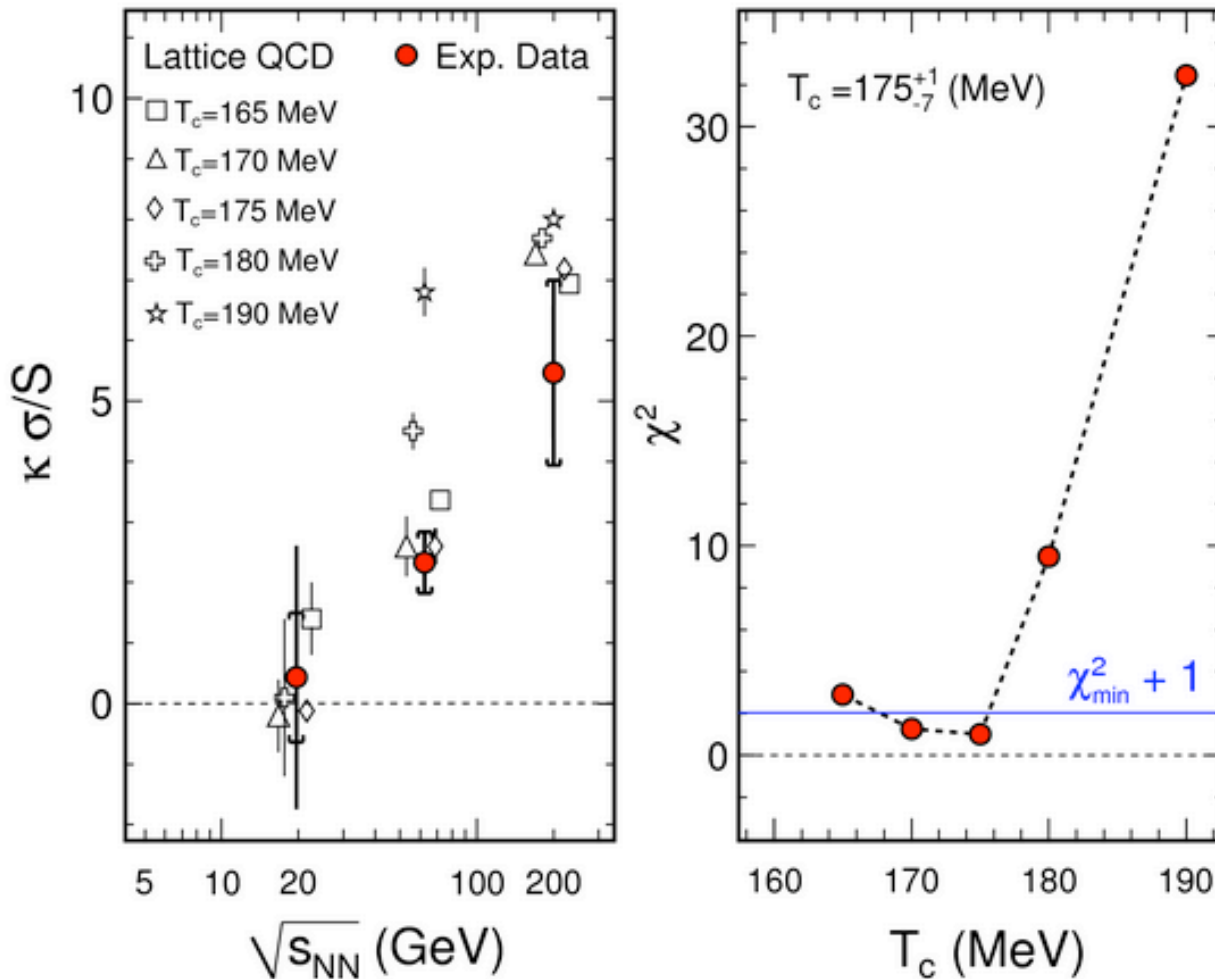
(b)

It is the temperature at the peak of a susceptibility related to the confinement-deconfinement order parameter

# Setting the scale of bulk QCD

$$\chi^{(4)} / [\chi^{(3)} T] \sim \text{Kurtosis} \times \sigma / \text{Skewness}$$

S. Gupta, X. Luo, H. G. Ritter,  
BM, N. Xu



$T_c$  compatible with

- ✓ Indirect estimates  
(Scale via Hadronic observables)
- ✓ Temperature scales  
from resonance gas  
models

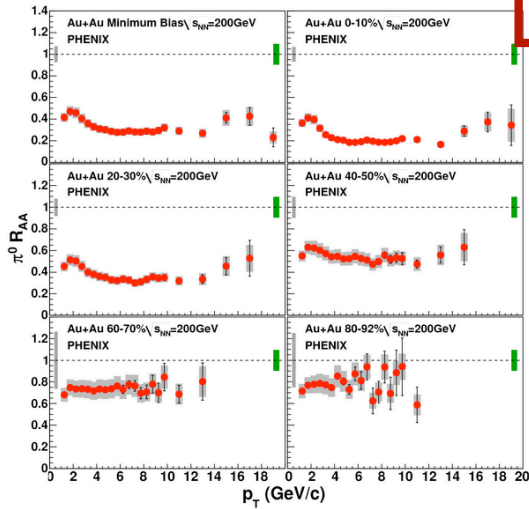
$$T_c = 175^{+1}_{-7} \text{ MeV}$$

$$\chi^2(T_c) = \sum_{\sqrt{s_{NN}}} \frac{[m_3^{\text{expt}}(\sqrt{s_{NN}}) - m_3^{\text{QCD}}(\sqrt{s_{NN}}, T_c)]^2}{\text{Error}_{\text{expt}}^2 + \text{Error}_{\text{QCD}}^2}$$

# Searching the phase boundary

PHENIX : PRL 101, 232301  
(2008)

Au+Au 200 GeV

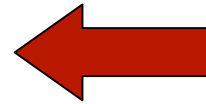


Jet quenching

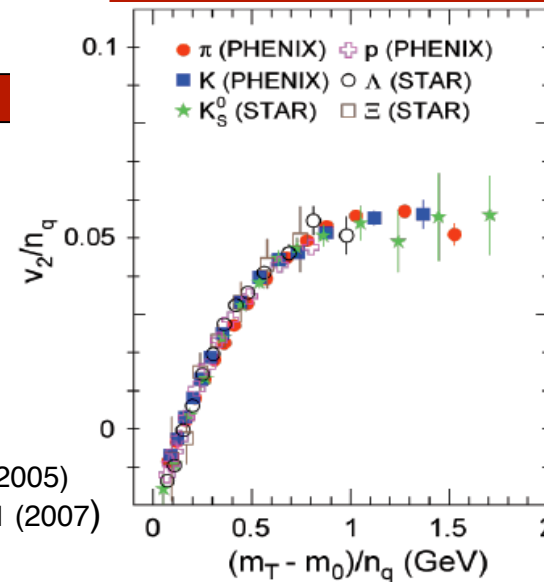


No Jet Quenching

No NCQ Scaling  
 $\phi$   $v_2$  small

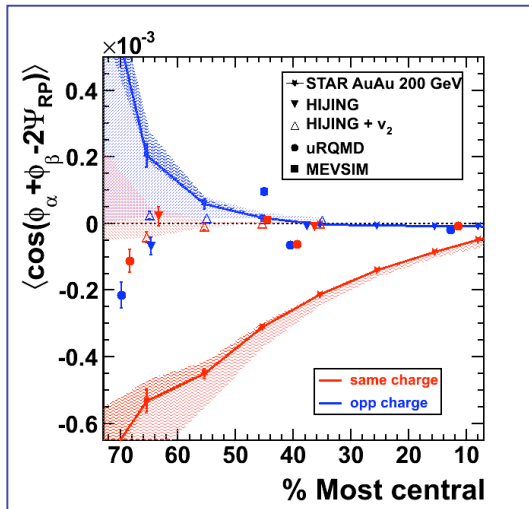


Partonic collectivity

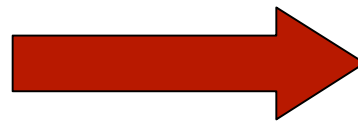


STAR, PRL 95, 122301 (2005)  
PHENIX, PRL 98, 162301 (2007)

Chiral Magnetic effect



STAR:PRL 103 (2009) 251601;  
STAR: 0909.1717



No Dynamical Charge  
Asymmetry

# Search For The QCD Critical Point

*In the fields of observation chance favors only the prepared mind.  
Louis Pasteur*

## Strategy:

- (I) Establish observables for Critical Point which has sound theoretical basis and reflects the signatures at CP.
- (II) Expectations from the observable from non critical point physics should be understood.
- (III) Vary beam energy of collisions and look for non-monotonic dependence of the observable.

# Signature Of Critical Point



$T > T_c$     $T \sim T_c$     $T < T_c$

Critical Opalescence as observed in  $\text{CO}_2$  liquid-gas transition

T. Andrews.

Phil. Trans. Royal Soc., 159:575, 1869

- Distributions become non Gaussian
- Correlation length diverges
- Susceptibilities diverges
- Long wavelength fluctuations or low momentum fluctuations important

Deviation

$$\delta N = N - \langle N \rangle$$

Standard deviation,  $\sigma = \sqrt{\langle (\delta N)^2 \rangle}$

**Skewness**  $= \frac{\langle (\delta N)^3 \rangle}{(\sigma)^3}$

**Kurtosis**  $= \frac{\langle (\delta N)^4 \rangle}{(\sigma)^4} - 3$



# Higher Moments of Net-Protons

## Distributions non Gaussian at CP

Moments and Correlation length ( $\xi$ )

$$\langle (\delta N)^2 \rangle \sim \xi^2 \quad \langle (\delta N)^3 \rangle \sim \xi^{4.5}$$

$$\langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2 \sim \xi^7$$

Value limited in heavy-ion collisions

Finite size effects  $\xi < 6$  fm

Critical slowing down, finite time effects  $\xi \sim 2 - 3$  fm

Higher moments higher sensitivity

M. A. Stephanov, PRL 102, 032301 (2009)

Y. Hatta et al, PRL 91, 102003 (2003)

## Link to Lattice QCD and QCD Models

Kurtosis x Variance  $\sim \chi^{(4)} / [\chi^{(2)} T^2]$

Skewness x Sigma  $\sim [\chi^{(3)} T] / [\chi^{(2)} T^2]$

R. Gavai & S. Gupta, arXiv:1001.3796

## Net-proton Number Fluctuations

$\sim$  Singularity in charge and baryon number susceptibilities

$$Q = B/2 + I_3$$

$$\chi_Q \sim (1/VT) \langle (\delta Q)^2 \rangle = (1/4) \chi_B + \chi_I$$

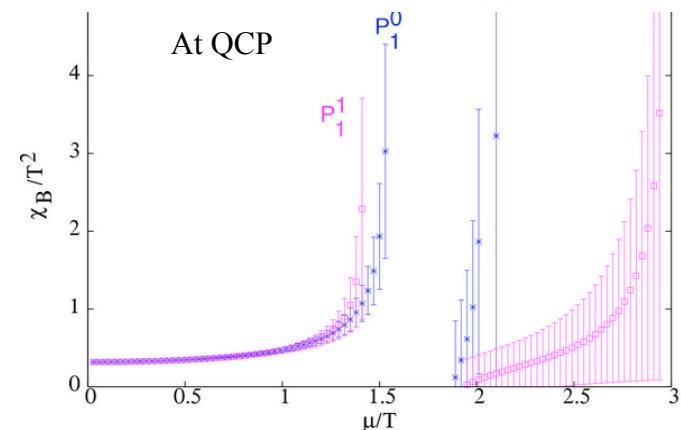
$$\sim (1/VT) \langle \delta (N_{p-pbar})^2 \rangle$$

## iso-spin blindness of $\sigma$ field

M. Cheng et al, PRD 79, 074505 (2009)

B. Stokic et al, PLB 91, 192 (2009)

R. Gavai & S. Gupta PRD 78, 114503 (2008)

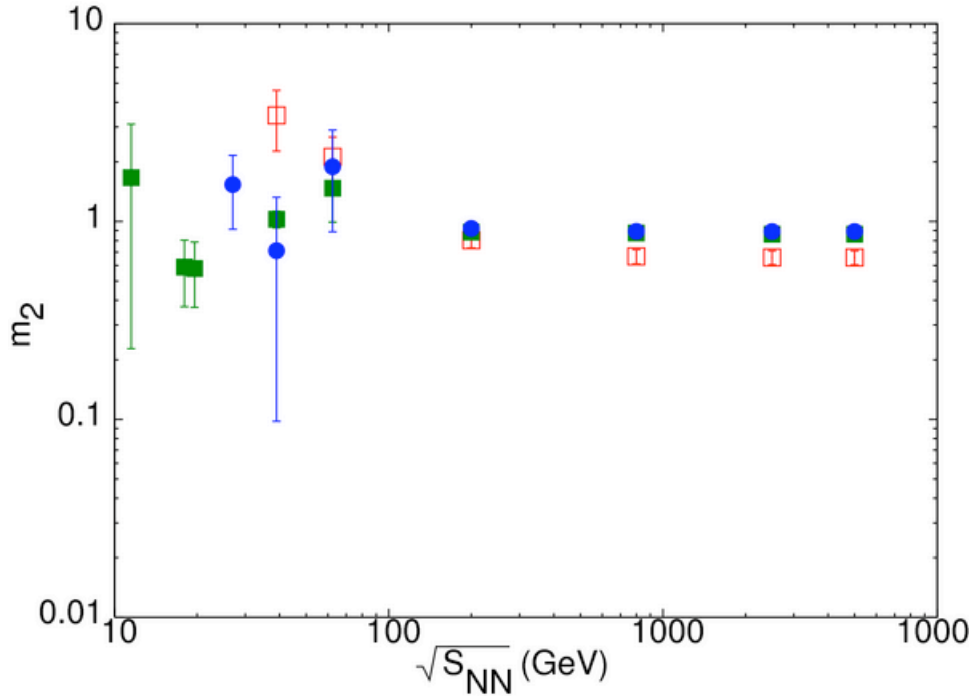


Non monotonic variation of products of higher moments with beam energy

# Theory Expectations

## Lattice QCD

(R. Gavai, S. Gupta, arXiv:1001.3796)

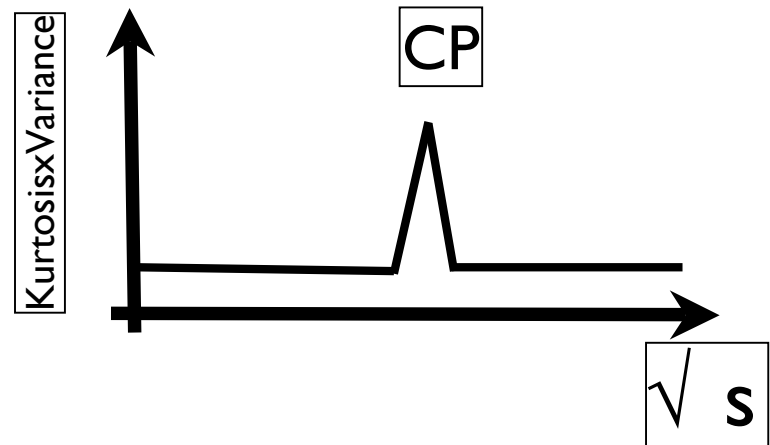


$m_2$  equivalent to Kurtosis x Variance  
At CP : Kurtosis x Variance has large values

## CP Model

(C. Athanasiou, M. Stephanov, K. Rajagopal, arXiv:1006.4636 and PRL 102 (2009) 032301)

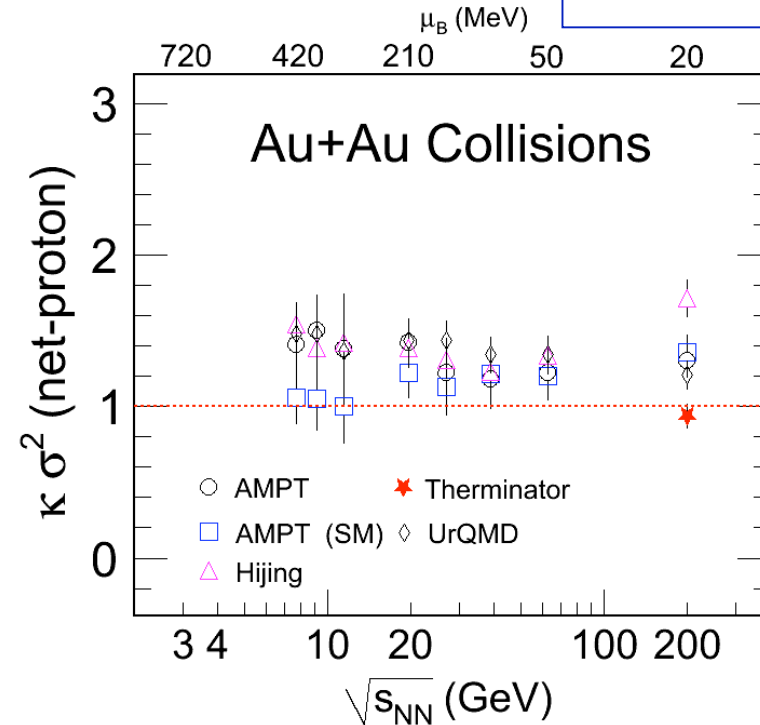
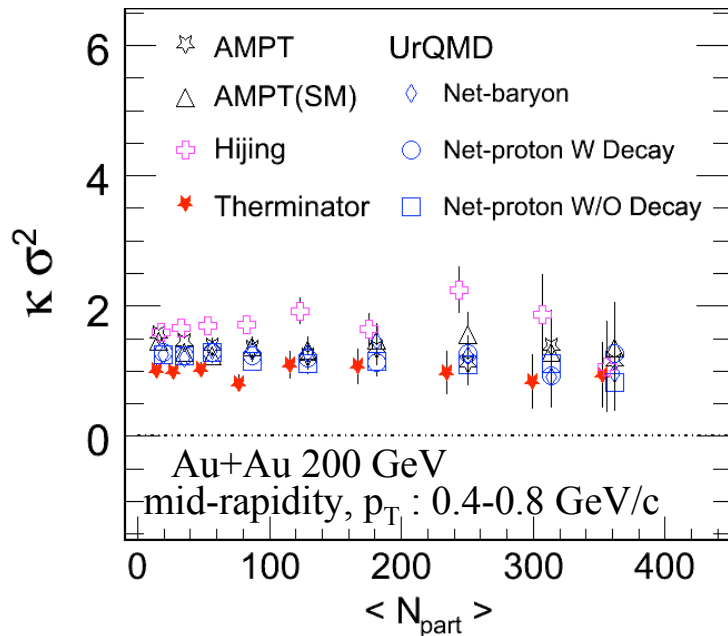
Beam Energy (GeV)	Kurtosis x Variance (net protons) with $\xi \sim 3\text{fm}$ and CP (No CP $\sim 1$ )
200	$\sim 2.5$
62	$\sim 35$
19	$\sim 3700$
7.7	$\sim 29600$



# Observable: non-CP Physics

Beam energy

Collision centrality

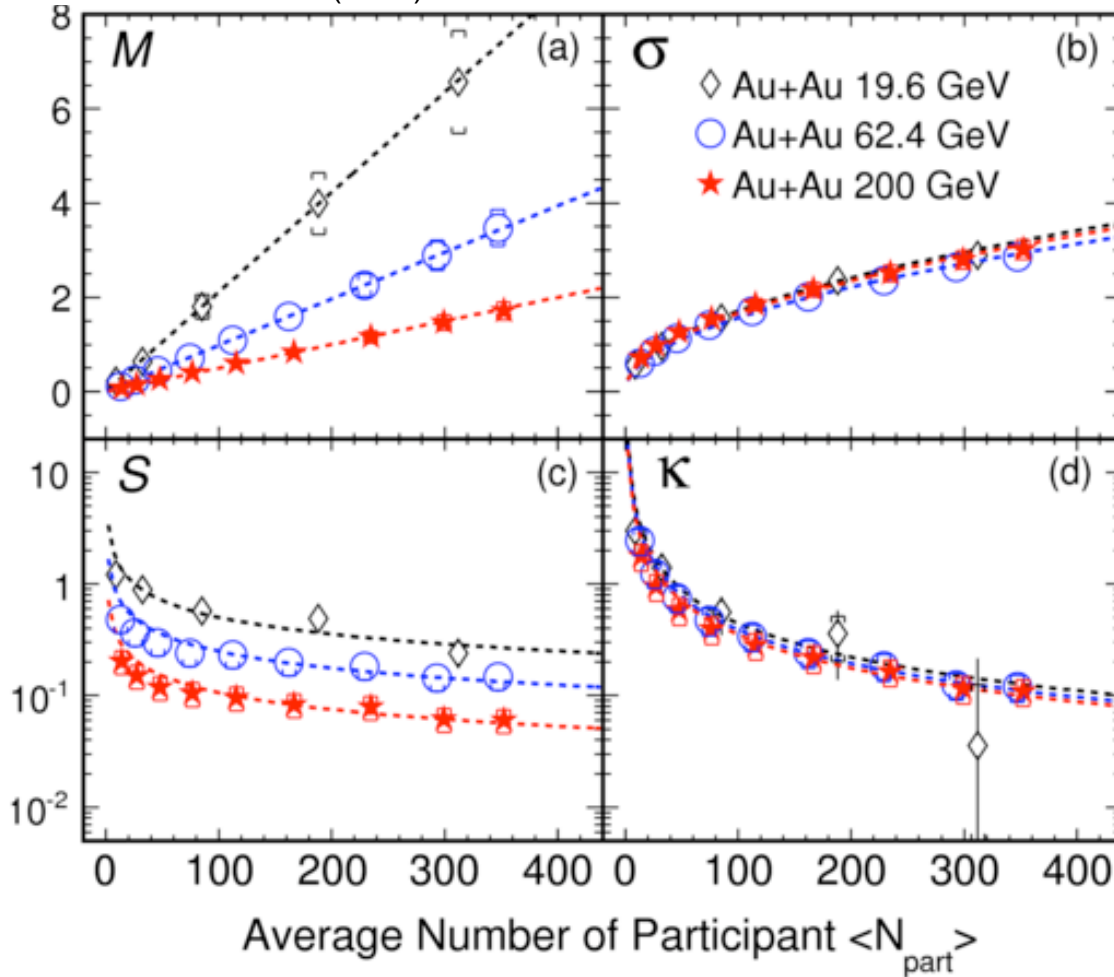


## Kurtosis x Variance: (Desirable features for CP Search)

- o Constant as a function of beam energy
- o Constant as a function of collision centrality/impact parameter
- o No difference between net-baryon and net-proton
- o Effect of resonance decay small
- o Similar values for Transport, Mini-jets, Coalescence models
- o Unity for Thermal model

# Moments: Net-Proton Distribution

STAR: PRL 105 (2010) 022302



Moments:

$$\sigma = \sqrt{\langle (N - \langle N \rangle)^2 \rangle}$$

$$s = \frac{\langle (N - \langle N \rangle)^3 \rangle}{\sigma^3}$$

$$K = \frac{\langle (N - \langle N \rangle)^4 \rangle}{\sigma^4} - 3$$

Central Limit Theorem:

$$M_i = C M_x \langle N_{\text{part}} \rangle_i$$

$$\sigma_i^2 = C \sigma_x^2 \langle N_{\text{part}} \rangle_i$$

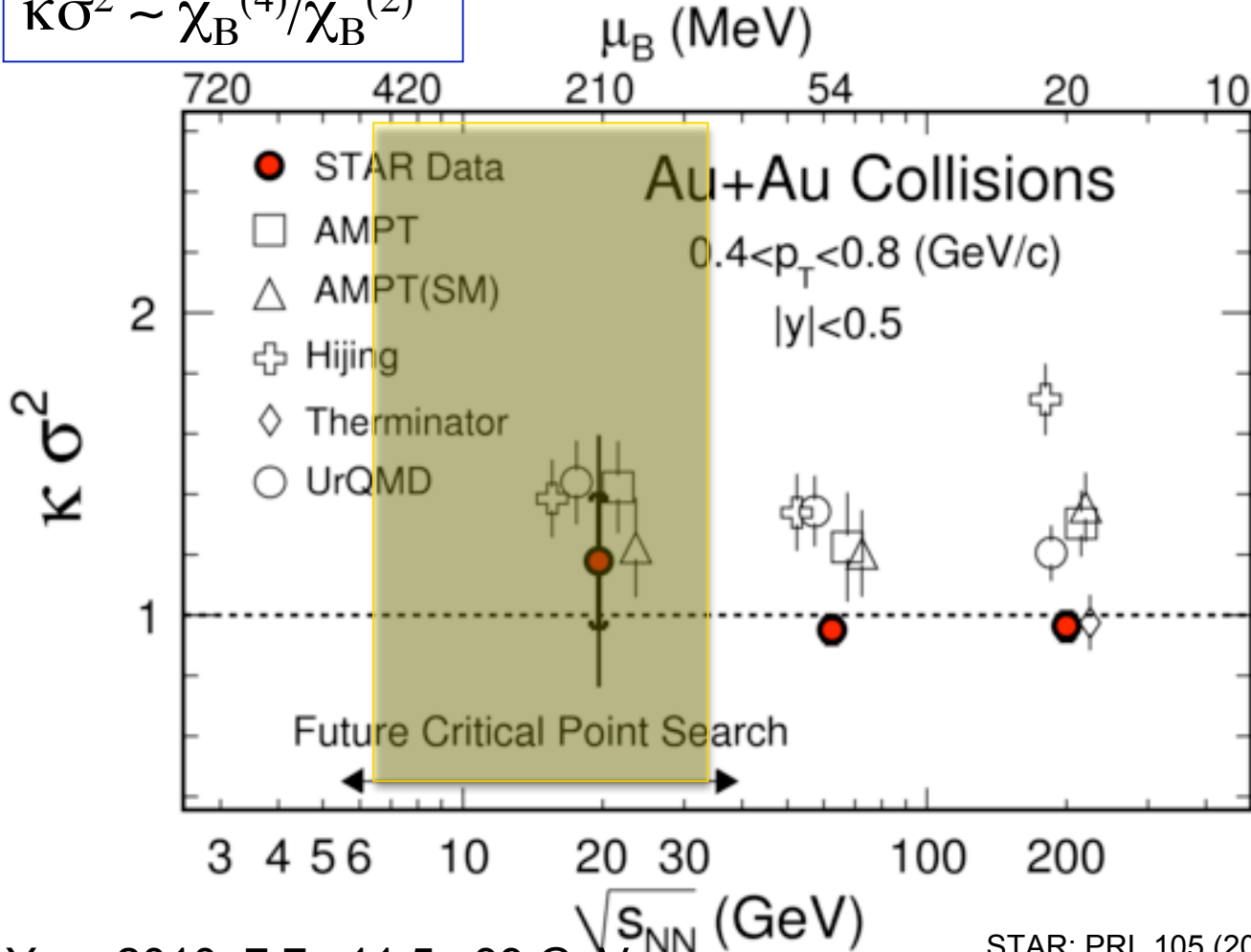
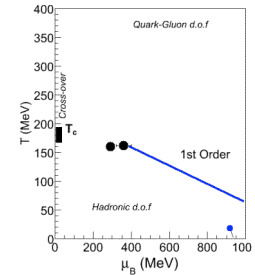
$$S_i = S_x / \sqrt{[C \langle N_{\text{part}} \rangle]_i}$$

$$K_i = K_x / [C \langle N_{\text{part}} \rangle]_i$$

Consistent with CLT expectations (lines)

# Energy Dependence: $\kappa\sigma^2$

$$\kappa\sigma^2 \sim \chi_B^{(4)}/\chi_B^{(2)}$$



CP Model:  $\kappa\sigma^2 > 2$

arXiv: 1006.4636;  
PRL 102 (2009) 032301

Models:

$\Delta\mu_B^C \sim 100 \text{ MeV}$

PRL 101 (2008) 122302;  
PLB 647 (2007) 431  
Eur. Phys. Lett. 86  
(2009) 31001

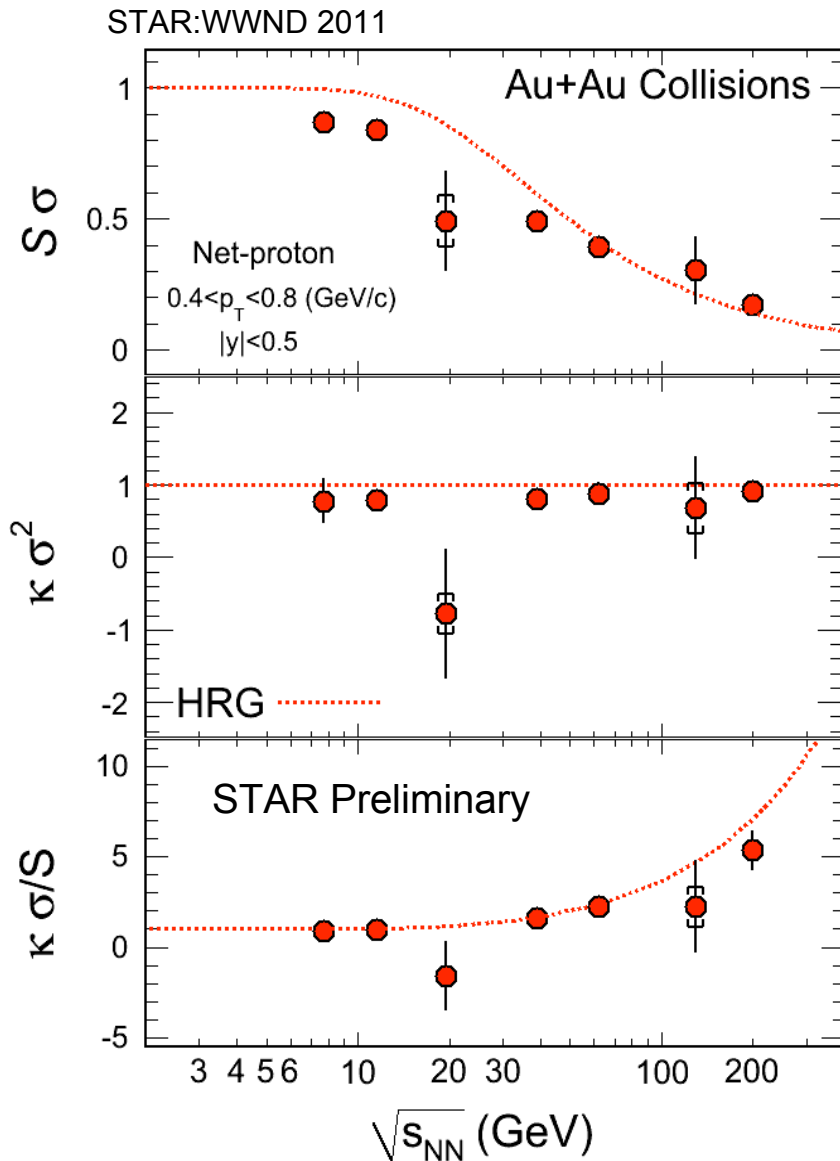
Year 2010: 7.7, 11.5, 39 GeV

Year 2011: 18, 27 GeV

STAR: PRL 105 (2010) 022302

Observations indicate CP not located for  $\mu_B < 200 \text{ MeV}$

# STAR: BES Results



Baryon number fluctuations:

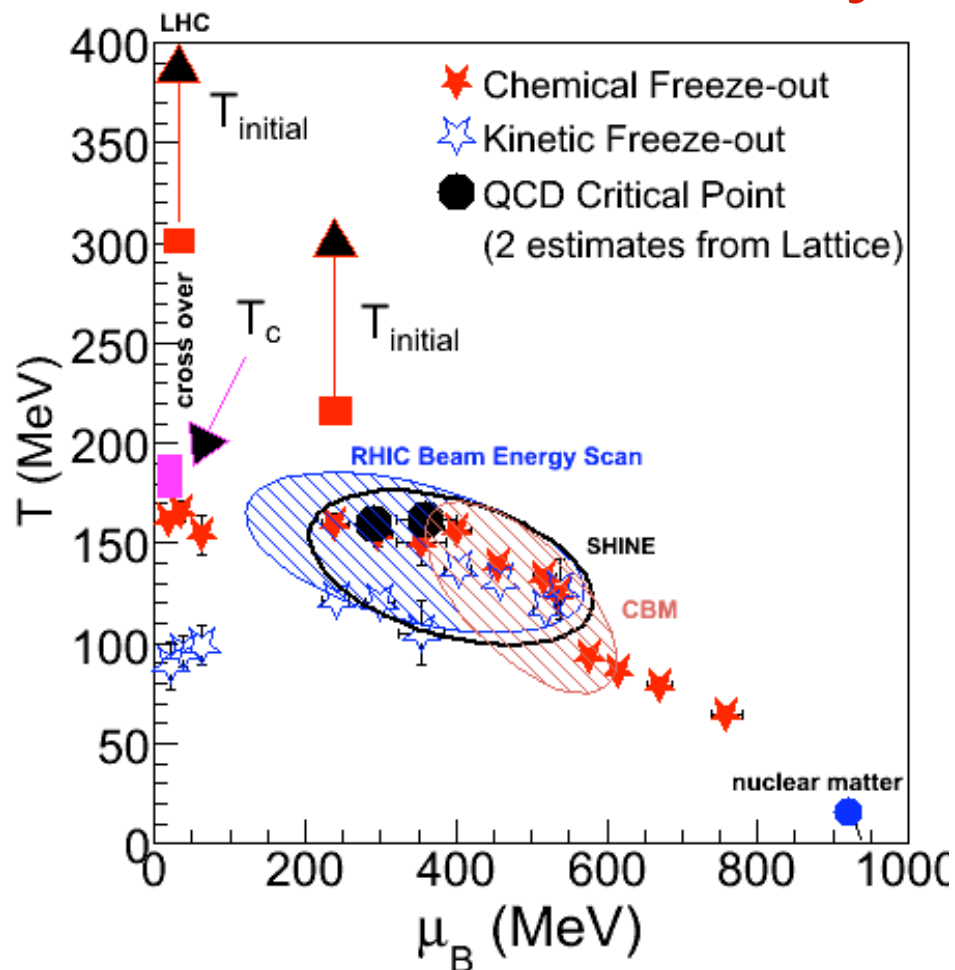
Thermalization  
 and/or

Deviation from Poisson fluctuations

Deviations from HRG from 39 GeV

Need high statistics run  
 at 18 GeV in context of CP search

# Summary and Outlook



With the starting of LHC ( $\mu_B \sim 0$ ) - we have unique opportunity to understand the properties of matter governed by quark-gluon degrees of freedom at unprecedented initial temperatures achieved in the collisions.

To make the QCD phase diagram a reality equal attention needs to be given to high baryon density region.

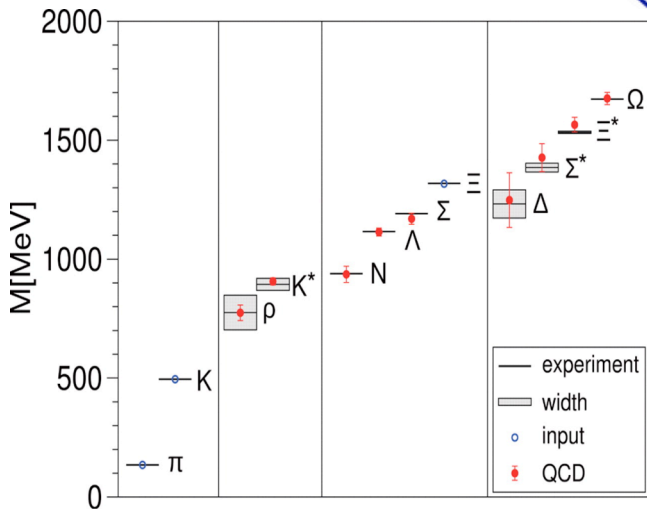
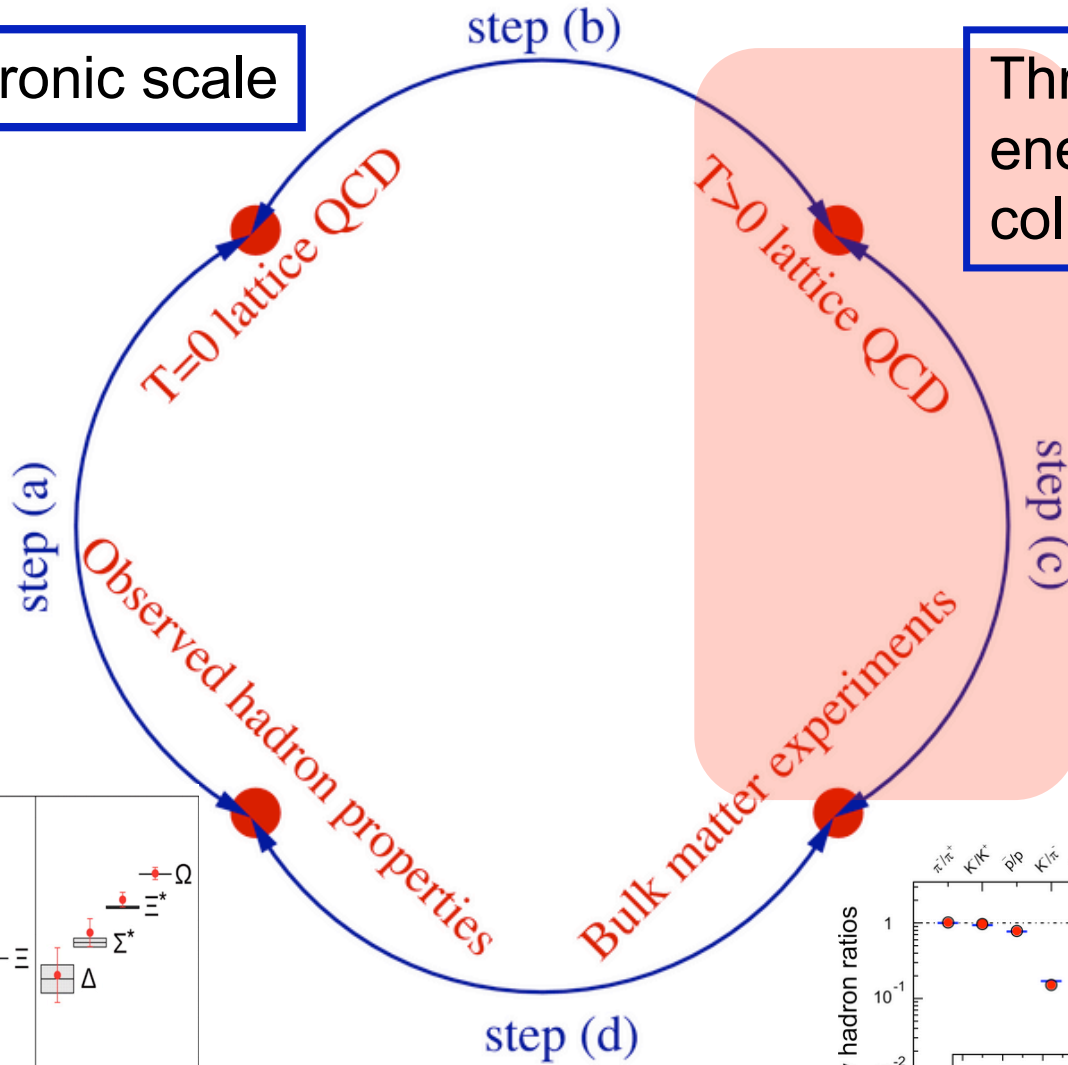
These two complementary programs will make our understanding clearer on:

- ✓ *Test of QCD in non-perturbative regime*
- ✓ *characterization of quark-gluon matter at varying baryon density*
- ✓ *searching for the QCD critical point and*
- ✓ *searching for the QCD phase boundary*

# Circle Of Reasoning

$T_c / m$ ;  $m = \text{hadronic scale}$

Through high energy nuclear collisions



$T_{ch} = 163 \pm 4 \text{ MeV}$   
 $\mu_B = 24 \pm 4 \text{ MeV}$

